

$$6+i \xrightarrow{\text{square it}} (6+i)^2 = (6+i)(6+i)$$

↓ N it

$$= 36 + 6i + 6i + \cancel{i^2}^{-1}$$

$$\begin{aligned} N(6+i) &= (6+i)(6-i) \\ &= 36 + 6i - 6i - i^2 \\ &= \underline{37} \end{aligned}$$

$$= \underline{35} + \underline{12i}$$

$$35^2 + 12^2 = 37^2 \text{ neat!}$$

$$m+ni \xrightarrow{\text{sq it}} \underline{(m^2-n^2)} + \underline{2mn}i$$

↓ N it

$$N(m+ni) = \underline{m^2+n^2}$$

$$\text{so is } (m^2-n^2)^2 + (2mn)^2 = (m^2+n^2)^2 ?$$

Week 1: What questions are rolling in our heads?

- Why can't 103 be written as $N(x+yi)$?
(x, y integers)
- What type of numbers give primitive Pythagorean triples?
- Why does the hypotenuse have to be written as x^2+y^2 ?
- Which N values can be produced by multiple positive pairs of x, y ?
- Is there a method that produces all Pythagorean triples?
- "Dude where's my isometric paper?" (60° triangles w/ integer sides)
- "Dudette, where's my $\sqrt{2}$?"
- "Whoa! N -values & geometry?"
- What's the plural of "hypotenuse"?